```
DATA bball;
INPUT Name $ 
CARDS;
<data goes here>
;
```

A) Why should we probably ignore the three fielding related statistics (PutOuts86, Assists86, and Errors86)?

## Because they depend on the position being played (as discussed in the first question of the take home exam).

B) Create a new data set that standardizes all of the carreer statistics to be yearly averages instead of totals, and that doesn't have the fielding statistics, position, league, or teams.

```
DATA bball2;
SET bball;
DROP AtBatsCar HitsCar HRCar RunsCar RBICar WalksCar PutOuts86 Assists86 Errors86 Pos86
League Team86 Team87;
AtBatAvg = AtBatsCar/Years;
HitsAvg = HitsCar/Years;
HRAvg = HRCar/Years;
RunsAvg = RunsCar/Years;
RBIAvg = RBICar/Years;
WalksAvg = WalksCar/Years;
RUN;
```

C) One way of analyzing the data would be to simultaneously attempt to predict each of the y variables from the optimal linear combinations of the x variables. Which type of analysis is this?

## This would be a multivariate multiple regression.

D) What is the best linear predictor of HR86 and RBI 86 using the standardized career numbers and years?

What is the p -value for testing that all of the slope coefficients involved are 0 ?

```
PROC REG DATA=bball2;
MODEL HR86 RBI86 = AtBatAvg HitsAvg HRAvg RunsAvg RBIAvg WalksAvg Years;
MTEST;
RUN;
```

[NOTE: As said in class, a blank MTEST line will simultaneously test the null hypothesis that all of the coefficients for predicting the Y variables from all of the X variables are 0 . If you had more Y or X variables than shown above, then you would need to list which ones you wanted to use for the test on the MTEST line.]

From the SAS output below we see that the best linear predictor of HR86 (after some rounding) is: 5.59-0.02 AtBatAvg + 0.04 HitsAvg + 1.26 HRAvg + 0.09 RunsAvg - 0.04 RBIAvg - 0.10 WalksAvg - 0.03 Years

## The best for RBI86 is:

27.21-0.05 AtBatAvg - 0.20 HitsAvg - 0.31HRAvg + 0.47 RunsAvg + 1.42 RBIAvg - 0.36 WalksAvg - 0.43 Years

The desired $p$-value is $<0.0001$ and we reject the null hypothesis that the set of $X$ variables and set of $Y$ variables are not linearly related.

E) Conduct a canonical correlation analysis for predicting the 86 batting statistics and 87 salary from the standardized career batting statistics and number of years.

This was done using PROC INSIGHT and PROC CANCOR.

```
PROC CANCORR DATA=bball2 VPREFIX=career WPREFIX=year86 ALL;
VAR AtBatAvg HitsAvg HRAvg RunsAvg RBIAvg WalksAvg Years;
WITH AtBats86 Hits86 HR86 Runs86 RBI86 Walks86 Salary87;
RUN;
```

What is the p -value for testing whether there is any linear relationship between the x variables and the y variables?

| Multivariate Statistics and F Approximations |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $S=7 \quad M=-0$ | $N=101$ |  |  |  |
| Statistic | Value | F Value | Num DF | Den DF | $\mathrm{Pr}>\mathrm{F}$ |
| Wilks' Lambda | 0.00354293 | 43.28 | 49 | 1040.1 | <. 0001 |
| Pillai's Trace | 3. 54520445 | 30.79 | 49 | 1470 | <. 0001 |
| Hotelling-Lawley Trace | 10.34665162 | 42.78 | 49 | 676.05 | <. 0001 |
| Roy's Greatest Root | 3.48908766 | 104.67 | 7 | 210 | <. 0001 |

How many of the pairs of canonical variates are significantly correlated? Report the test statistic and measure of effect size (that is, measure of how correlated).

All seven of the pairs of canonical variates are significantly correlated as can be seen from the p-values.

| Test of HO: CanCorr[j]=0, j>=K |  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: |
| K | L. Ratio | Approx F | Num DF | Den DF | Pr $>$ F |
| 1 | 0.003543 | 43.2777 | 49 | 1040.0957 | $<.0001$ |
| 2 | 0.015905 | 39.3237 | 36 | 902.9789 | $<.0001$ |
| 3 | 0.056030 | 35.9538 | 25 | 766.7580 | $<.0001$ |
| 4 | 0.152118 | 33.7180 | 16 | 633.0331 | $<.0001$ |
| 5 | 0.349713 | 30.3749 | 9 | 506.3680 | $<.0001$ |
| 6 | 0.610826 | 29.2080 | 4 | 418.0000 | $<.0001$ |
| 7 | 0.871233 | 31.0376 | 1 | 210.0000 | $<.0001$ |

The estimated correlations range from 0.359 to 0.882 .


Provide interpretations for the statistically significant canonical variates.

|  | Correlations Betwen the VAR Variables and Their Canonical Variables |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | career 1 | career 2 | career 3 | career 4 | career 5 | career 6 | career 7 |
| At Bat Avg | 0.2549 | -0.2662 | 0.5117 | 0.4919 | 0.2330 | -0. 0487 | 0.0705 |
| HitsAvg | 0.2568 | -0.3139 | 0.6371 | 0.4479 | 0.1553 | -0.4431 | 0.0925 |
| HRAvg | 0.8474 | -0. 3156 | -0.0236 | 0.3873 | 0.0318 | -0.1488 | -0.0927 |
| RunsAvg | 0.3169 | -0.1326 | 0.5410 | 0.6655 | 0.1433 | -0.3438 | 0.0879 |
| RBI Avg | 0.6712 | -0.4019 | 0.3641 | 0.3391 | 0.2714 | -0. 2551 | -0.0414 |
| WalksAvg | 0.5794 | 0.3672 | 0.5101 | 0.3519 | 0.1856 | -0.3331 | 0.0082 |
| Years | 0.3728 | -0.0503 | 0.1806 | -0.0873 | 0.2317 | -0.0695 | 0.8716 |
|  | Correlations |  |  |  |  |  |  |
|  | year 861 | year 862 | year 863 | year 864 | year 865 | year 866 | year 867 |
| At Bats 86 | 0.1583 | -0.3377 | 0.4223 | 0.5515 | 0.2358 | -0.4932 | -0.2819 |
| Hits 86 | 0.1405 | -0. 0.4011 | 0.5992 | 0.4809 | 0.0976 | -0.3481 | -0.3136 |
| HR 86 | 0.7528 | -0.3888 | -0.1052 | 0.4515 | -0.0706 | -0.0657 | -0.2405 |
| Runs 86 | 0.2463 | -0.1639 | 0.4645 | 0.7462 | 0.0788 | -0. 1527 | -0.3322 |
| RBI 86 | 0.5970 | -0.4869 | 0.2210 | 0.3743 | 0.3047 | -0.1024 | -0.3381 |
| Walks 86 | 0.5697 | 0.4043 | 0.4841 | 0.3226 | 0.2115 | -0.2780 | -0.2270 |
| Salary 87 | 0.4715 | -0.1810 | 0. 5742 | 0.2333 | 0.1603 | 0.0125 | 0.5787 |

The following are fairly rough interpretations ( 0.5 is generally used as a cut off when possible, but not always)... I wouldn't expect you to get the titles in bold unless you are a baseball person.

## Power Hitter Numbers (Home Runs, RBIs, and Walks)

Career 1 = Combination of Career Averages of Home Runs, RBIs, and Walks
Year86 1 = Combination of 1986 Home Runs, RBIs, and Walks (and possibly Salary in 87)

## Walks vs. Everything Else

Career 2 = Career Average in Walks contrasted with all the other Career Averages (not Years)
Year86 $2=1986$ Totals in Walks contrasted with all the other 1986 numbers (but not Salary in 87)

## Getting On Base

Career 3 = Career Average in At Bats, Hits, Runs, and Walks (Hits most)
Year 863 = 1986 Totals in At Bats, Hits, Runs, Walks, and Salary (Hits and Salary Most)

## Scoring Runs

Career 4 = Combination of all the Career Averages, but especially Runs (not Years)
Year86 4 = Combination of all 1986 numbers and Salary, but especially Runs

## Counting Everything But Home Runs

Career 5 = Weak average of everything but Home Runs
Year86 5 = Weak average of everything but Home Runs (Home Runs negative, Hits and Runs little weight)

## ????

Career 6 = At Bats and a little bit of everything else?
Year86 6 = At Bats and a little bit of everything else but Salary?

## Overpaid Old Guys

Career 7 = Years in league
Year86 7 = Salary vs. everything else

Are there any points in the plots of the canonical variates that are outliers? Which players are they?


4 Player 210 = Wade Boggs

V Player 141 = Mike Schmidt


