

# STAT 530/J530 November 15<sup>th</sup>, 2005

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## So Far

### Principal Components

- Produces an orthogonal representation of the original data
- Allows counting the number of dimensions that explain the most variation in the original data set
- No statistical model
- Works for interval scale data



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## So Far

### Factor Analysis

- Fits a model to explain the observed variables in terms of underlying latent factors
- Lots of options
- Is a linear model that requires interval data
- Some procedures require multivariate normality



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## So Far

### Multidimensional Scaling

- Provides a graphical display of high dimensional data in fewer dimensions
- Can work with any kind of data if the appropriate distance measure is used
- Classical method is equivalent to principal components
- Non-metric methods allow for presenting more groups in fewer dimensions and better focus on small distances



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## So Far

### Cluster Analysis

- Provides a graphical display of high dimensional data by producing a dendrogram of various clusters.
- Can work with any kind of data if the appropriate distance measure and linkage are used
- No definitive way of choosing the right number of clusters.



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## So Far

### MANOVA

- Provides a test of the hypothesis that several populations have the same mean vector
- Assumes multivariate normality, equal covariances, and independence
- This often isn't the actual question of interest



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## So Far

### Discriminant Analysis

- Finds the linear combinations of variables that best distinguishes between the groups of interest
- Works with any interval data
- Is the optimal procedure if the data is multivariate normal with equal covariances
- Provides posterior probabilities assuming the equal covariance normality



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## So Far

### Logistic Regression

- Predicts group membership from interval scale variables
- If the logistic curve is appropriate it provides a test of the hypothesis similar to MANOVA
- If the logistic curve is appropriate it provides a predicted group membership
- Does not require multivariate normality



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## Next

Today: Overview of multiple regression and introduction to canonical correlation analysis

Thursday 17<sup>th</sup>: Homework 8 is due, canonical correlation analysis continued

Tuesday 22<sup>nd</sup>: Brief homework 9 is due, final exam is posted, begin optional topic and course evals



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## Next

Thursday 24<sup>th</sup>: Thanksgiving – No Class

Tuesday 29<sup>th</sup>: Optional topic continued

Thursday 1<sup>st</sup>: Homework 10 is due, ice cream field trip as penance for Homework 6 grade being late! With time for questions while we eat.

5:30pm Tuesday, December 6<sup>th</sup> – Final Exam is Due



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## Motivating Data Set

Consider the energy crisis data...

Factors that affect transportation decisions

- **Economy**
- **Convenience**
- **Low Energy Use**
- **Dependability**



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## Motivating Data Set

Views on the Energy Crisis

- **Q1 - If the energy shortage gets any worse, the country will be in bad shape.**
- **Q4 - Saving energy requires you to make major sacrifices.**
- **Q6 - Utility companies should be allowed to burn cheaper fuel even though this would cause more pollution.**
- **Q9 - Rationing of energy resources will be necessary for at least the next five years.**
- **Q10 - Conserving electricity will save me money in the long run.**



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## Motivating Data Set

- Q13 - There is not much an average citizen can do to save electricity.
- Q17 - We should forget about reducing pollution until our energy problems are solved.
- Q18 - My personal conservation efforts have little impact on total consumption of energy.
- Q19 - Because of the abundance of coal, industries should be encouraged to switch to coal as a fuel despite the air pollution it causes.



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## The Question

How do the answers to the survey questions relate to the factors determining what kind of transportation people use?



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## Multiple Regression

$$y_i = \beta_0 + \beta_1 x_{i1} + \dots + \beta_q x_{iq} + \varepsilon_i$$

Where the  $\varepsilon$  are

- Normally distributed
- Have mean zero
- Have constant variance
- Are independent



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