

$$\log(\frac{p}{1-p}) = \beta_0 + \beta_1 x$$

$$p=P[Y=1]=\frac{e^{(\beta_0+\beta_1x)}}{1+e^{(\beta_0+\beta_1x)}}=\frac{1}{1+e^{-(\beta_0+\beta_1x)}}$$