

Statistics 516 - Spring 2002 - Final Exam Solutions (*modified for Spring 2003 Practice*)

Part I:

- 1) The errors must be normally distributed, have mean zero, and equal variances at each treatment level, and must be independent.
- 2) The probability of observing a test statistic as extreme as the one observed, or more extreme, if the null hypothesis is true.

Part II:

- 1)  $H_0: \beta_{\text{walk}}=0$  given that the bank clerk speed is also included in the model  
vs.  $H_A: \beta_{\text{walk}} \neq 0$  given that the bank clerk speed is also included in the model  
where  $\beta_{\text{walk}}$  is the coefficient for the average walking speed
- 2)  $SSE=951.6389-212.8264= 738.8125$      $df=35-3=32$      $MSE=738.8125/32= 23.0879$
- 3) Chattanooga has the largest DFITs (0.9755), we compare this to  $2\sqrt{(m+1)/n}=2\sqrt{(3+1)/36}=2/3$  and see that it would have a significant effect on the model.
- 4) The model with bank and walk has  $C_p < k+1$ , has the fewest variables of any such model, and has the highest adjusted  $R^2$
- 5)  $y_{ijk} = \mu_{\text{base}} + \alpha_i + \gamma_j + (\alpha\gamma)_{ij} + \epsilon_{ijk}$   
 $y_{ijk}$  = the  $k^{\text{th}}$  observation in specialty  $i$  and city  $j$      $\mu_{\text{base}}$  = the baseline mean  
 $\alpha_i$  = the main effect due to specialty  $i$      $\gamma_j$  = the main effect due to city  $j$   
 $(\alpha\gamma)_{ij}$  = the interaction due to specialty  $i$  and city  $j$      $\epsilon_{ijk}$  = the error for the  $k^{\text{th}}$  observation in specialty  $i$  and city  $j$
- 6) The treatment effects for Pediatrics and Diabetes & Hypertension are equal. ( $\gamma_{\text{Ped}} = \gamma_{\text{DnH}}$ )
- 7) The interaction between specialty and city is not significant (p-value=0.9877)
- 8) Modified Levene Test or Brown and Forsythe Test
- 9) No significant difference (p-value=0.5368).
- 10) There is a significant effect (p-value=0.0467) and the estimated average change is -0.0364 for each additional year.
- 11)  $R^2 = 0.3429$  so 34.29%
- 12) No. The p-value for the interaction is 0.0287.
- 13) Yes. We fail to reject the null hypothesis that it is appropriate with a p-value of 0.6714 from the Hosmer and Lemeshow Goodness-of-Fit test.
- 14) Yes. We reject the null hypothesis that they are not related with a p-value of 0.0006 from the Likelihood Ratio = Deviance test.
- 15)  $P[\text{survive} = 1] = \frac{1}{1 + e^{-(59.2919 - 0.3677(200))}} = \text{approximately } 0$   
(notice that the slope is negative!)
- 16) We are extrapolating.