

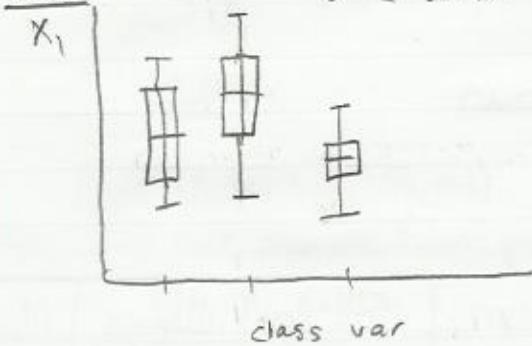
## Chapter 3 Diagnostics

- Check for outlying predictor variables w/ boxplots

CODE: proc boxplot;

```
plot Xi*classVar/boxstyle=schematic; run;
```

OUTPUT:



- Residuals:  $e_i = Y - \hat{Y}_i$   
 $s^2(e_i) = \frac{\sum(e_i - \bar{e})}{n-2} = \frac{\sum e_i^2}{n-2} = \text{MSE}$   
not independent Random Variables
- Studentized Residuals:  $e_i^* = \frac{e_i - \bar{e}}{\sqrt{\text{MSE}}} = \frac{e_i}{\sqrt{\text{MSE}}}$
- We need to check for these problems
  - 1) The regression function isn't linear
  - 2) The error terms do not have constant variance
  - 3) The error terms are not independent
  - 4) The model fits all but one or a few outlier observations
  - 5) error terms not normally dist
  - 6) One or several important predictor variables have been omitted from the model

### Problem One: Non-linearity of regression function

Check using:

- ① Scatterplot: look for a linear pattern

CODE Proc sgscatter;  
plot y\*x/loess;  
run;



- ② Residual Plot: look for no pattern: balanced around 0

CODE Proc glm;  
model y=x;  
output out=glmData r=r;  
run;  
Proc sgscatter data=glmData;  
plot r\*x;  
run;



### Problem Two: Nonconstant variance of errors

- ① Residual Plot: there should be no megaphone shape

- see code above

- ② Absolute value of residuals Plot: There should be no pattern or triangle shape

CODE: Proc Glm plots=all;  
model y=x;  
output out=glmData r=r;  
run;

data glmDataAbs;  
set glmData;  
absr = Abs(r);  
run;

proc sgscatter data=glmDataAbs;  
plot absr\*x;  
run;



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### Problem Three Presence of outliers

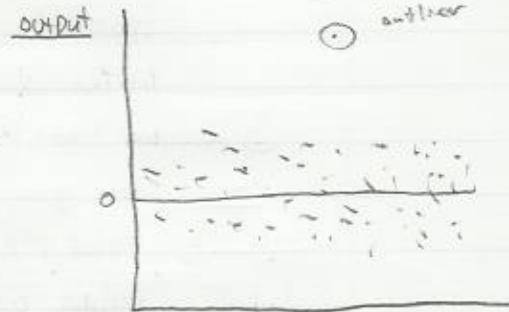
Check using:

① Box plot - see earlier code

② Studentized Residuals vs. predictor: look for points far from cloud for outlying observations

CODE

```
proc glm;
model y=x;
output out=glmData rstudent:rs;
run;
proc sgscatter data=glmData;
plot rs*x;
run;
```



### Problem four Non independence of error terms: plot residuals in order

of time taken, there should be no patterns

CODE

```
proc glm;
model y=x;
output out=glmData r=r;
run;
proc sgscatter;
plot r*sequence-variable;
run;
```



### Problem five Non-normality of error terms

① Boxplot - see earlier code: should be symmetric, no outliers

② QQ Plot - Given in glm diagnostics - should fit straight line

③ Histogram - Given in glm diagnostics - should look approx normal

If you don't like graphs there are tests! ☺

Brown Forsythe Test - Tests for statistically constant variance across groups

CODE

```
proc glm;
  class class-var;
  model y = class-var;
  means class-var/hortest=BF;
run;
```

NOTE: Does not depend on normality of error terms

Output

Source	DF	Sum of Squares	Mean Square	Fvalue	Pr > F
class-var				$\frac{MS_C}{MS_E}$	P value for constant var
error					

Breusch Pagan Test - Tests for constant variance

CODE:

```
proc model;
  parms beta0 beta1;
  y = beta0 + beta1*x;
  fit y / breush=(1 x);
run;
```

Note: Assumes normal & independent errors

Equation	Test	Statistic	DF	Pr > ChiSq	Variables
	Breushagan			test for constant variance	1, x

(1)

## Normality tests

Shapiro-Wilk: dependent on sample size

Kolmogorov-Smirnov: dependent on vertical distance of  $F_x(x)$  and  $F_{normal}(x)$

Cramer-von Mises: uses empirical distribution functions  $\rightarrow$  Quadratic EOF

Anderson Darling: Based on Square Difference

Code proc univariate Normal;      Output

Var X;  
run;

Test	Statistic	p value
Shapiro-Wilk	W	
Kolmogorov-Smirnov	D	
Cramer-von Mises	W <sub>sq</sub>	
Anderson Darling	A-g	

F test for Lack of Fit 'Test if model fits data well'

- Assumes:
  - independent & normal errors
  - constant variance

Code proc reg;  
model y=x/lackfit;  
run;

Output

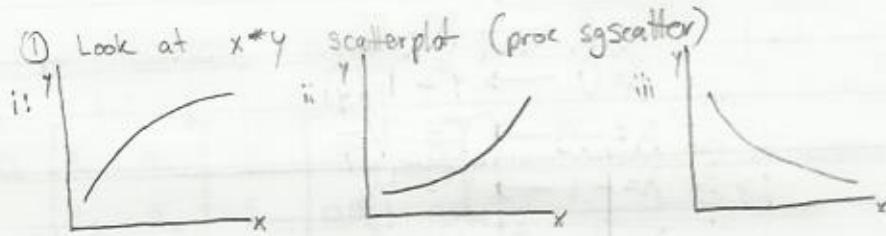
Source	DF	Sum of squares	Mean squares	F value	Pr>F
Model					(all coeff = 0 p value)
Error					
Lack of fit					Test regression function is linear
Pure error					
(corrected total)					

(14)

- How to fix Nonlinearity of regression function
  - ① Add interaction terms  
i.e.  $y_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \epsilon_i$
  - ② Transform data to make it linear, or more linear
- How to fix nonconstancy of error variance
  - ① Weighted least squares
  - ② Transform data to make it more constant
- How to fix Nonindependence of error terms
  - ① Use a model that allows this
- How to fix non normality of Error terms
  - ① Transform data to make errors more normal
- How to fix outlying observations
  - ① Disregard if they're not representative

### Transformations

- To fix non linear relations; if error terms are approximately normal we want to transform  $x$ , not  $y$



② Transform  $x$

$$\text{i: } x^* = \sqrt{x}$$

$$x^* = \ln(x)$$

$$\text{ii: } x^* = x^2$$

$$x^* = e^x$$

$$\text{iii: } x^* = \frac{1}{x}$$

$$x^* = e^{-x}$$