

STAT 535: Chapter 8(a):  
In Which the Class Enjoys a Brief Yet Fascinating  
Interlude to Discuss Prior Elicitation

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- ▶ A challenge is putting “expert opinion” into a form where it can be used as a prior distribution.

## **Strategies:**

- ▶ Requesting guesses for several quantiles (maybe  $\{0.1, 0.25, 0.5, 0.75, 0.9\}$ ?) from a few experts.
- ▶ For a normal prior, note that a quantile  $q(\alpha)$  is related to the z-value  $\Phi^{-1}(\alpha)$  by:

$$q(\alpha) = \text{mean} + \Phi^{-1}(\alpha) \times (\text{std. dev.})$$

- ▶ Via regression on the provided  $[q(\alpha), \Phi^{-1}(\alpha)]$  values, we can get estimates for the mean and standard deviation of the normal prior.

- ▶ Another strategy asks the expert to provide a “predictive modal value” (most “likely” value) for the parameter.
- ▶ Then a rough 67% interval is requested from the expert.
- ▶ With a normal prior, the length of this interval is twice the prior standard deviation.
- ▶ For a prior on a Bernoulli probability, the “most likely” probability of success is often “clear”.