For all these problems, show fully how you got your answers!

1. The following table summarizes the race and positions of NBA players in 1993.

|  |  | Position |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Guard | Forward | Center | Totals |  |
|  | Race: | White | 26 | 30 | 28 |
|  | Black | 128 | 122 | 34 | 284 |
|  | Totals | 154 | 152 | 62 | 368 |

Suppose one player is chosen at random from this group. Let us define the following events:
$A=\{$ the selected player is white $\}$
$B=\{$ the selected player is a center $\}$
$\mathrm{C}=\{$ the selected player is black $\}$
$\mathrm{D}=\{$ the selected player is a guard $\}$
(a) Find $\mathrm{P}(\mathrm{A})$.
(b) Find $\mathrm{P}(\mathrm{B})$.
(c) Find $\mathrm{P}(\mathrm{C} \cap \mathrm{D})$.
(d) Find the probability that the player is NOT a guard.
(e) Find $\mathrm{P}(\mathrm{A} \cup \mathrm{B})$.
2. For two independent events $A$ and $B$, suppose $P(A)=0.4$ and $P(B)=0.2$.
(a) Find $\mathrm{P}(\mathrm{A} \cap \mathrm{B})$.
(b) Find $\mathrm{P}(\mathrm{A} \mid \mathrm{B})$.
(c) Find $\mathrm{P}(\mathrm{A} \cup \mathrm{B})$.
3. Define the two events A and B as follows:
$A=\{$ we have rain tomorrow $\}$ and $B=\{$ we have 10 -plus mph wind tomorrow $\}$.
Assume $\mathrm{P}(\mathrm{A})=0.4, \mathrm{P}(\mathrm{B})=0.2$, and $\mathrm{P}(\mathrm{A} \cap \mathrm{B})=0.1$.
(a) What is the probability that we have at least one of either rain or $10-\mathrm{mph}$ wind tomorrow?
(b) What is the probability of rain tomorrow, given that we have 10 - mph wind?
(c) Are events A and B independent? Give a mathematical justification for your answer.
4. (a) Suppose events $A$ and $B$ are independent and that $P(A)=0.3$ and $P(B)=0.4$. What is $\mathrm{P}(\mathrm{A} \cup \mathrm{B})$ ? What is $\mathrm{P}(\mathrm{A} \mid \mathrm{B})$ ?
(b) Are A and B mutually exclusive events? Why or why not?
5. In a country club, $60 \%$ of the members use the golf course, $80 \%$ use the tennis courts, and $5 \%$ use neither facility. For a randomly selected member, consider events $\mathrm{G}=\{$ uses the golf course \} and $\mathrm{T}=\{$ uses the tennis courts \}.
(a) Given that a randomly selected member uses the tennis courts, what is the probability that this member uses the golf course?
(b) Based on your answer to part (a), are T and G independent events? Why or why not?

Answers: (1) a) .2283 b) .1685 c) .3478 d) .5815 e) .3207 (2) a) .08 b) .4 c) .52
(3) a) .5 b) .5 c) No (4) a) $.58, .3$ b) No (5) a) .5625 b) No

